8.1 Harder Similarity Area Problems

Example
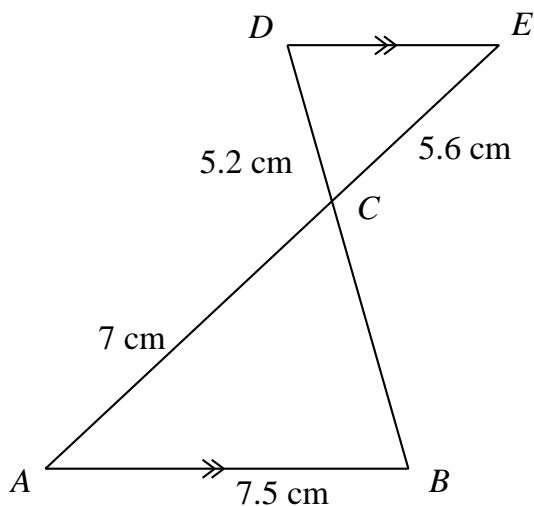*GCSE Examination Question from 2013, paper 4H, Q17 (Edexcel)*

Diagram **NOT**
accurately drawn

AB is parallel to *DE*
The lines *AE* and *BD* intersect at *C*
AB = 7.5 cm, *AC* = 7 cm, *CD* = 5.2 cm, *CE* = 5.6 cm
(**a**)   Calculate the length of *BC*

[**2 marks**]

(**b**)   Calculate the length of *DE*

[**2 marks**]

(**c**)   The area of triangle *ABC* is 21 cm²
Calculate the area of triangle *EDC*

[**3 marks**]

8.2 Exercise

Question 1

Let OA = 8 cm, AX = 4 cm and AB = 6 cm

$\triangle OAB$ has an area of 40 cm^2

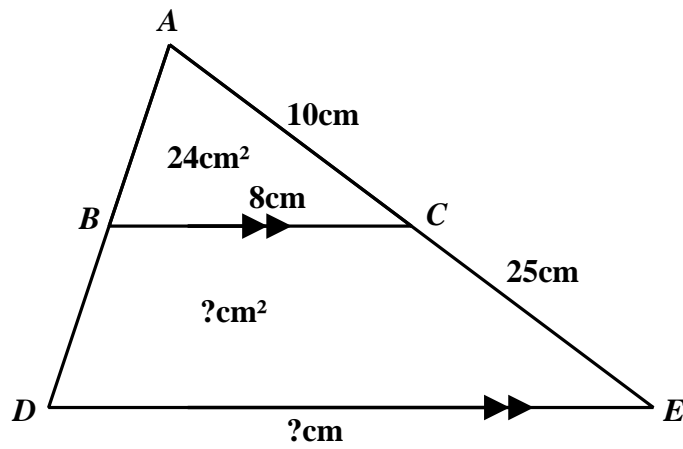Find the length of XY and the area of the trapezium $AXYB$
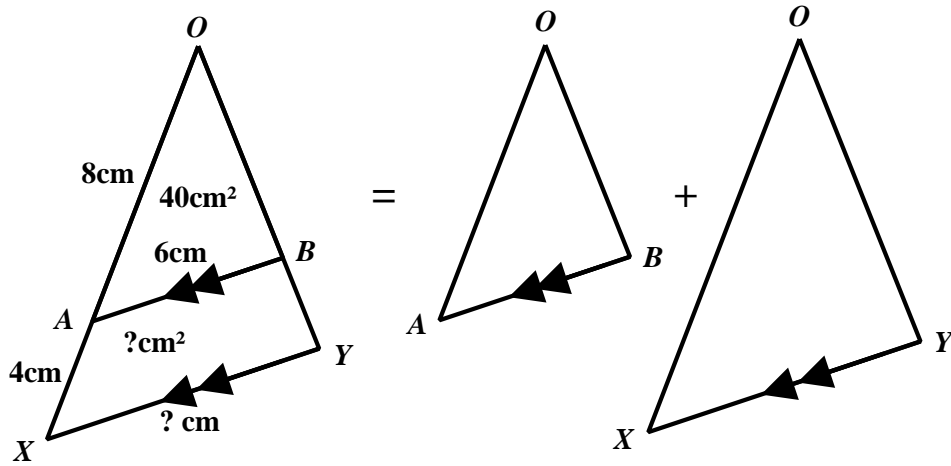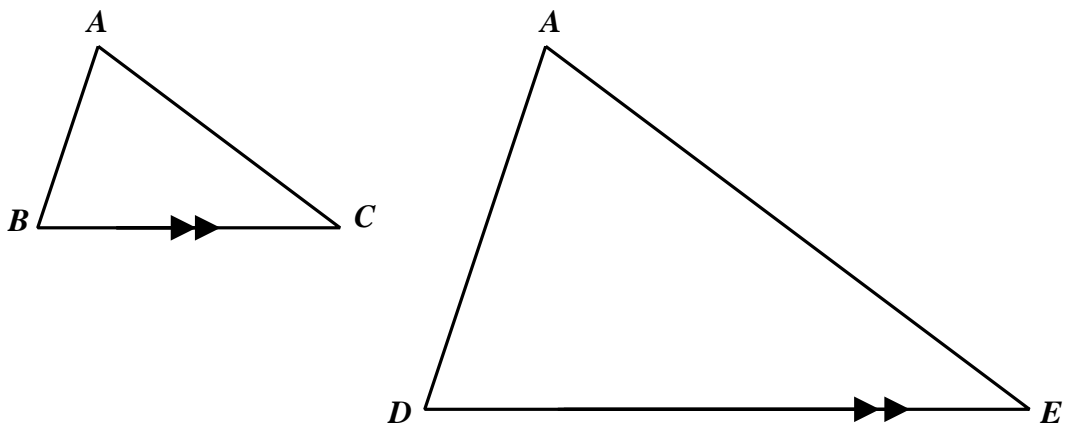

[6 marks]

Question 2

In the diagram below, $AC = 10$ cm, $BC = 8$ cm and $CE = 25$ cm.

The area of $\triangle ABC$ is 24 cm ^{2}.

BC is parallel to DE.

(**i**)   Transfer the relevant measurements from the above diagram onto the one below which shows the two similar triangles separated.

[**2 marks**]

(**ii**)   Find the length of DE and the area of the trapezium $BDEC$
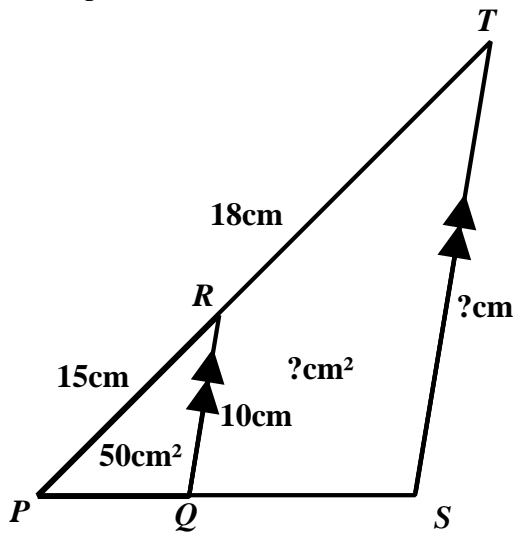
[**4 marks**]

Question 3

In the diagram below, $PR = 15$ cm, $RT = 18$ cm and $QR = 10$ cm.

The area of $\triangle PQR$ is 50 cm²

QR is parallel to ST

Find the length of ST and the area of the trapezium $QRTS$.

Question 4

In this question give your answers in the form $\frac{p}{q}$ in as simple a form as possible where p and q are integers and $q \neq 0$

What is the *length scale factor* that maps;

(i)   A length of 12 cm onto a length of 15 cm ?

[1 mark]

(ii)   A length of 21 cm onto a length of 24 cm ?

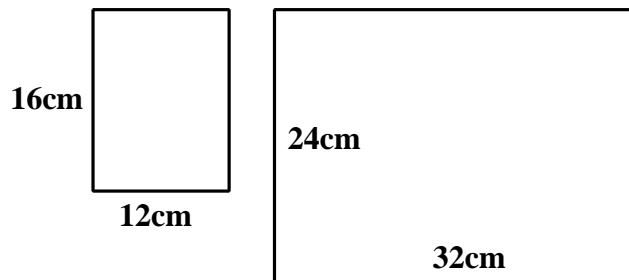[1 mark]

(iii)   A length of 45 cm onto a length of 63 cm ?

[1 mark]

Question 5

The following two rectangles are similar.
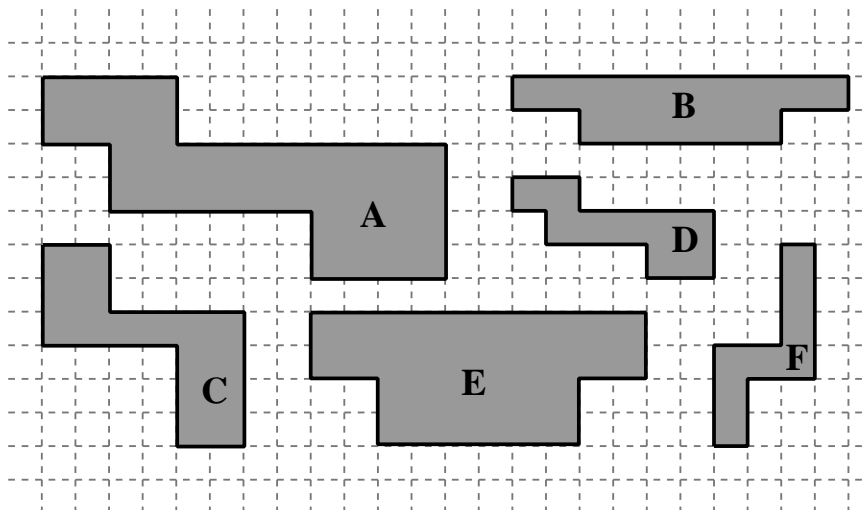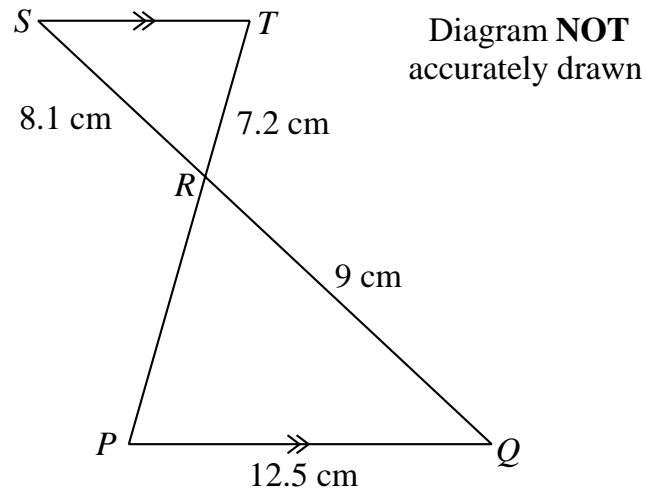What is the length scale factor between them ?
HINT : Be careful !

16cm

12cm

24cm

32cm

[2 marks]

Question 6

Which two of the following shapes are similar ?

[2 marks]

Question 7

Diagram **NOT**
accurately drawn

PQ is parallel to *ST*
The lines *PT* and *QS* intersect at *R*
PQ = 12.5 cm, *QR* = 9 cm, *SR* = 8.1 cm, *TR* = 7.2 cm

(**a**) Calculate the length of *PR*

[2 marks]

(**b**) Calculate the length of *ST*

[2 marks]

(**c**) The area of triangle *PQR* is 36 cm²
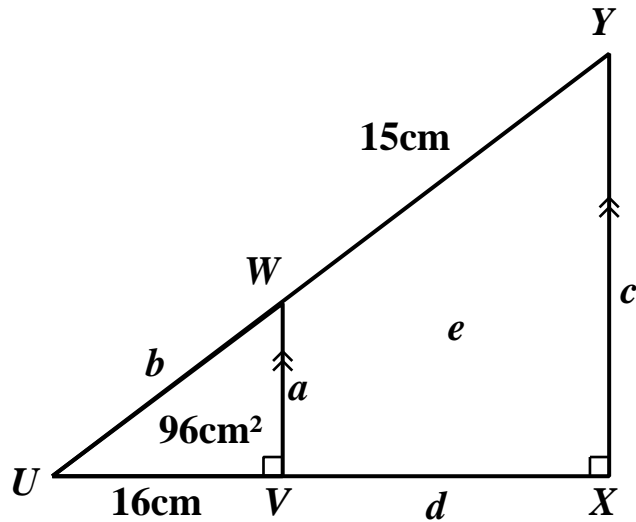Calculate the area of triangle *RTS*

[3 marks]

Question 8

In the diagram below, $UV = 16$ cm, and $WY = 15$cm
The area of $\triangle UVW$, which is right angled, is 96 cm^2
VW is parallel to XY

(**i**)   Find the length of VW, UW, XY then VX

(**ii**)   Find the area of the trapezium $VWYX$
Good luck with this A* grade question.