Chapter 4

A-Level Pure Mathematics Vectors II : Year 1 and Year 2

4.1 Vectors: Topic Summary

Question 1

In a desert exercise a tank travels 12 km on a bearing of 070° from an Oasis, *O*, then 14 km on a bearing of 160° to a Bunker *B*.

(i) Provide a sketch of the tank's manovers marking on the following; 12 km, 14 km, O, B, 70° , 90°

[2 marks]

(ii) Determine the bearing of the tank's bunker location from the Oasis.

[2 marks]

A regular hexagon has its six vertices marked O, A, X, Y, Z, and B as shown.



[3 marks]

Question 3

A yacht is initially at the position, $Y_A = -3i - j$ km. Some time later it is at position, $Y_B = 4i - 2j$ km.





[2 marks]

(**ii**) By using the theorem of Pythagoras, and your part (i) answer, determine the distance across the sea-bed that the yacht has covered.

[2 marks]

Two motor boats, *The Chunter* and *The Rapid* sit side by side upon the ocean. They then separate, each at a constant velocity. *The Chunter* has velocity $V_C = 3 i + 5 j$ kmh⁻¹ *The Rapid* has velocity $V_R = 8 i + 4 j$ kmh⁻¹ (i) Calculate the speed of *The Chunter*.

[2 marks]

(ii) How far will *The Chunter* travel in 2 hours 15 minutes ?

[2 marks]

(iii) Calculate the velocity of *The Chunter* relative to *The Rapid*.

[2 marks]

(iv) Use your part (iii) answer to calculate, in hours and minutes, how long it will take until the two motor boats are 8 km apart.

[2 marks]

Question 5

A particle *P* has velocity (3i + 2j) ms⁻¹ when t = 0 seconds and velocity (7i + 4j) ms⁻¹ at time t = 2 seconds Find the acceleration of *P* assuming that it is constant.

[4 marks]

The position of a particle at time *t* is given by;

$$r = (3t - 7)i + (6t + 1)j$$

(i) If *d* is the distance in metres of *r* from the origin at time *t*, find an expression for *d* that involves the square root of a quadratic equation in *t*. (HINT : Pythagoras)

[2 marks]

$$\frac{1}{5}d^2 = 9\left(t - \frac{1}{3}\right)^2 + 9$$

[2 marks]

(iii) What value of t makes
$$\frac{1}{5} d^2$$
 as small as possible ?
This is the time at which the particle is closest to the origin.

[1 mark]

[1 mark]

At 11:00 hour the position vector of an aircraft relative to an airport *O* is; $r_A = (200 i + 30 j)$ km Note that *i* and *j* are unit vectors due east and due north respectively. The constant velocity of the aircraft is; $V_A = (180 i - 120 j)$ kmh⁻¹

Find;

(i) the time when the aircraft is due east of the airport O

[2 marks]

(**ii**) how far it then is from O

[2 marks]

(iii) how far it is from O at 12:00

[2 marks]