Lesson 12

A-Level Pure Mathematics, Year 1 Additional Mathematics Coordinate Geometry

12.1 Revision

Any solution based entirely on graphical or numerical methods is not acceptable Marks Available : 65

Question 1

The equation of a circle is;

$$(x + 7)^{2} + (y - 3)^{2} = 81$$

State the coordinates of the circle's centre, and its radius

[2 marks]

Question 2

Write down the equation of the circle with centre (5, 12) and which passes through the origin.

[2 marks]

Question 3

By completing the square, or otherwise, determine the centre and radius of the following circle;

$$x^2 + y^2 + 10x - 6y + 18 = 0$$

[5 marks]

Question 4 Differentiate (i)

 $y = 7x^{11} - 5x^3$ [2 marks]

(ii)

$$y = 24 x^{0.25}$$

[2 marks]

(iii)

$$y = \frac{4}{5}x^{-5}$$

[2 marks]

Question 5

The equation of the curve, plotted on the next page, is

$$y = \frac{x^3}{24} - x$$

(**i**) Write down the gradient equation, $\frac{dy}{dx}$, for the curve

[2 marks]

(ii) Use your part (i) answer to find the value of the gradient on the curve when x = 6

[1 mark]

(iii) Use your part (ii) answer to determine the equation of the tangent to the curve at the point (6, 3)

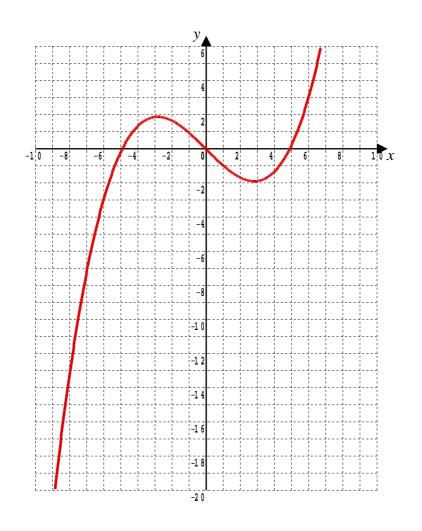
(iv) Use your part (ii) answer to determine the gradient of the normal to the curve at the point (6, 3)

[1 mark]

(v) Find the equation of the normal to the curve at the point (6, 3)

[2 marks]

(vi) On the graph, add your part (iii) tangent, and your part (v) normal, clearly indicating which is which and making sure they both pass through the point (6, 3)



[2 marks]

Question 6

$$(x+1)^2 + y^2 = 9^2$$

Is the point (5, 7) inside, outside, or on the circumference of this circle ? Justify your answer.

[3 marks]

Question 7

Find the point(s) of intersection, if any, of the circle

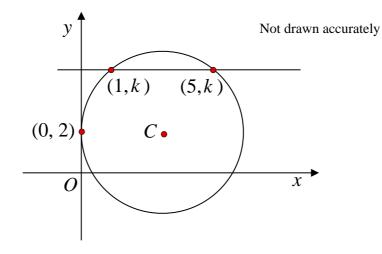
$$(x - 3)^{2} + (y + 2)^{2} = 13$$

and the line

y = 3x - 2

Question 8

Further Mathematics Specimen Examination Question 2020, Paper 1, Q11 (AQA) A circle, centre C, touches the y-axis at the point (0, 2)The line y = k intersects the circle at the points (1, k) and (5, k)



Work out the equation of the circle

[3 marks]

Question 9

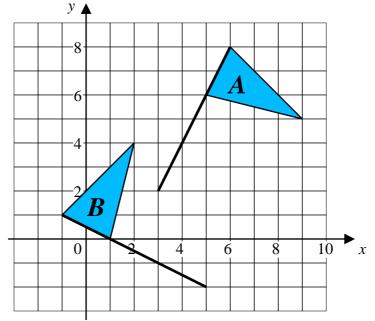
Find the coordinates of the point on the curve $y = (4x - 5)^2$ such that the gradient of the normal to the curve is $\frac{1}{8}$

Question 10

The diagram shows a flag A

The image of flag A when it is rotated by 90° is flag B

This question walks you through the steps involved in mathematically finding the centre of the rotation.



(i) Step 1:

Pick two matching points, say the foot of each flag pole, (3, 2) and (5, -2) **Step 2**:

Find the midpoint of these two points.

[1 mark]

(ii) Step 3:

Find the gradient of the straight line between these two points.

[1 mark]

(iii) Step 4:

Use the answers to Steps 2 and 3 to determine the equation of the perpendicular bisector of the two points.

(iv) Step 5 :

Pick two other matching points, say the tip of the flag, (9, 5) and (2, 4) **Step 6**:

Find the equation of the perpendicular bisector between these two points.

[4 marks]

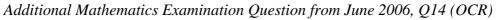
(v) Step 7:

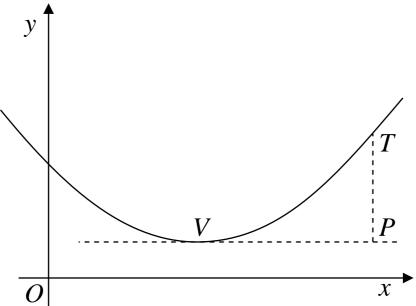
Find the point of intersection of the two perpendicular bisectors. This is the centre of the rotation.

[4 marks]

Check your mathematics is correct by using tracing paper, and verifying that when rotated by 90° about the point you claimed was the answer, flag A does indeed map onto flag B

Question 11





The diagram shows the quadratic curve

$$y = x^2 - 4x + 5$$

V(2, 1) is the minimum point of the curve.

T(5, 10) is a point on the curve.

The line VP is the tangent to the curve at V and TP is perpendicular to this line.

(i) Write down the coordinates of *P*

(ii) Find the coordinates of *M*, the midpoint of *VP*

[2 marks]

[1 mark]

(iii) Find the equation of the tangent of the curve at T

(iv) Show that the tangent to the curve at T passes through the point M

[2 marks]

(v) Use the result in part (iv) to suggest a way of drawing a tangent to a point on a quadratic curve without involving calculus.

[3 marks]

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