## Lesson 2

GCSE Mathematics
Angles \& Polygons

### 2.1 Irregular Polygons

- A polygon is a "many sided flat shape"
- It has interior (on the inside) angles and exterior (on the outside) angles.


## Example

This Quadrilateral has interior angles of $67^{\circ}, 160^{\circ}, 50^{\circ}$ and $83^{\circ}$
Notice that $67+160+50+83=360$


- For any polygon the sum of the interior angles depends upon how many sides it has, as shown in the following table;

| Polygon's <br> Name | Number <br> of Sides | Interior <br> Angle's Sum |
| :---: | :---: | :---: |
| Triangle | 3 | 180 |
| Quadrilateral | 4 | 360 |
| Pentagon | 5 | 540 |
| Hexagon | 6 | 720 |
| Septagon | 7 | 900 |
| Octagon | 8 | 1080 |
| Nonogon | 9 | 1260 |
| Decagon | 10 | 1440 |

- Here is a formula which some students like to learn that, given the number of sides in a convex polygon, works out the Interior Angle Sum;

$$
\begin{aligned}
& \text { Interior Angle Sum (Convex Polygon) } \\
& \qquad I A S=180(n-2)
\end{aligned}
$$

where $I A S$ is the Interior Angle Sum
and $\quad n$ is the number of sides

### 2.2 Exercise

You may use a calculator
Marks Available : 35

## Question 1

(i) What do the interior angles of a triangle add up to ?
( ii ) The following triangle is not drawn accurately; it's just a sketch. Use arithmetic to calculate the unknown angle marked $x$


## Question 2

(i) What do the interior angles of a quadrilateral add up to ?
[ 1 mark]
( ii ) The following quadrilateral is not drawn accurately; it's just a sketch. Use arithmetic to calculate the unknown angle, marked $y$


## Question 3

(i) What do the interior angles of a pentagon add up to?
( ii ) The following pentagon is not drawn accurately; it's just a sketch. Use arithmetic to calculate the unknown angle, marked $z$


## Question 4

(i) What do the interior angles of a hexagon add up to ?
( ii ) The following hexagon is not drawn accurately; it's just a sketch.
Use arithmetic to calculate the unknown angle, marked $x$


## Question 5

(i) Find angle $z$ in this isosceles triangle

( ii ) What does the following symbol on the triangle indicate ?

[ 1 mark]

## Question 6

(i) What do the interior angles of a septagon add up to?
[ 1 mark ]
( ii ) The following septagon is not drawn accurately; it's just a sketch. Use arithmetic to calculate the unknown angle, marked $x$


## Question 7

Find angle $w$ in this isosceles triangle


## Question 8

If a polygon the sum of the interior angles is $1440^{\circ}$
How many sides has the polygon?

## Question 9

Find angle $v$ in this isosceles triangle


## Question 10

What will the interior angles of a polygon with 22 sides sum to ? Give a reason for your answer.

## Question 11

A polygon has interior angles that sum to $2160^{\circ}$
How many sides has the polygon?
Give a reason for your answer.

## Question 12

Find angle $m$ in this isosceles triangle

[ 2 marks ]

## Question 13

A regular pentagon has five interior angles which are all the same size, and five sides which are all the same length.


Find angle $C$, the size of one interior angle, in a regular pentagon.

