## Lesson 5

## GCSE Mathematics

Set Theory II

### 5.1 Revision

Marks Available : 100

## Question 1

List the elements of the following sets;
(i) $Q=\{$ The factors of 18$\}$

$$
Q=\{
$$

$\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ \}
( ii ) $R=\{$ The factors of 12$\}$

$$
R=\{
$$

$\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ \}
( iii ) $\quad Q \cap R$

$$
Q \cap R=\{
$$

$\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ \}

## Question 2

Explain each of the following symbols;
(i) $\varnothing$
( ii ) $\notin$
(iii) $\cup$

Question 3
For each Venn Diagrams use set notation to describe the shading.


## Question 4

Let $\quad S=\{$ The first six multiples of 6$\}$
$F=\{$ Factors of 36\}
$T=\{$ The first eight triangular numbers $\}$
(i) List the elements of set $S$
$S=\{$ $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ \}
( ii ) List the elements of set $F$
$F=\{$ $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ \}
( iii ) List the elements of set $T$

$$
T=\{
$$

$\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$
$\qquad$
(iv) Complete the Venn diagram to show the relationship between $S, F$ and $T$


List all elements, if any, that are in the following intersections.
(v) $S \cap F=\{$ $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ \}
( vi) $\quad S \cap F \cap T=\{$ $\qquad$ , $\qquad$ \}
( vii) $S \cap F \cap T^{\prime}=\{$ $\qquad$ , $\qquad$ \}
( viii) $F \cap T^{\prime} \cap S^{\prime}=\{$ $\qquad$ , $\qquad$ , $\qquad$ \}
(ix ) What is $n(S \cup F)$ ? $\qquad$

## Question 5

A group of 45 teenagers were asked if they cleaned their teeth that morning.
They were also asked if they combed their hair.
Here is a summary of their answers :
$\diamond 38$ said they cleaned their teeth.
$\diamond 29$ said they combed their hair.
$\diamond 23$ said they had had both cleaned their teeth and combed their hair.
(i) Complete the Venn Diagram to clarify the teenagers' replies:

( ii ) How many teenagers neither cleaned their teeth nor combed their hair?
[ 6 marks ]

## Question 6

In a class of children, $G$ is the set of girls and $F$ is the set of those who like football. Shade the part that represents:
On (i) girls who like football.
On ( iii ) boys who like football.
(i)

(ii)

On ( ii ) girls who dislike football.
On (iv) boys who do not like football.

( iii )

(iv )


## Question 7

Set $M=\{$ Names of seasons in a year $\}$
What is $n\{$ Names of seasons in a year $\}$ ?

## Question 8

TRUE or FALSE?
(i) $n\{$ factors 21$\}=4$
(ii) $\quad n\{$ factors of 17$\}=2$
( iii ) $n\{$ factors of an even number $\}=3$
( iv ) $n\{$ factors of square number $\}=3$
( v ) $\quad n\{$ common factors of 15 and 24$\}=3$

## Question 9

In this question,

$$
\begin{gathered}
L=\{\text { Objects made from the metal lead }\} \\
B=\{\text { Types of balloon }\}
\end{gathered}
$$

(i) Describe the set $L \cap B$ in words.
(ii) If $L \cap B=\varnothing$, describe what this means.

## Question 10

In this question, consider all the positive integers.
Within this consideration, $P=\{$ Prime numbers $\}$
$C=\{$ Composite numbers $\}$
Describe in words the set $P \cup C$

## Question 11

Let : $A$ be the set of numbers in the infinite sequence $4,8,12,16,20, \ldots$ $B$ be the set of numbers in the infinite sequence $2,6,10,14,18, \ldots$
(i) List the a few members of the set $A \cup B$
( ii ) What is the special name given to the set $A \cup B$ ?
( iii) Describe $A \cap B$

## Question 12

In a class of 30 pupils,
$\diamond 18$ say they like pancakes.
$\diamond 13$ say they like maple syrup.
$\diamond 6$ say they do not like either pancakes nor maple syrup.
(i) Draw a Venn Diagram to clarify what the pupils say.
(ii) How many of the pupils like both pancakes and maple syrup?

## Question 13

Let $\quad S=$ \{Square numbers $\}$

$$
F=\{1,4,16,64,256,1024\}
$$

( a ) (i) List some elements of set $S$
(ii) Describe set $F$ in words
(b) For each of the following, decide if the given statement is TRUE or FALSE.
(i) $25 \in S$
( vi ) $\quad S \cup F=S$
( ii ) $1024 \notin S$
( vii ) $\pi \in S^{\prime}$
( iii) $64 \in S \cap F$
( viii ) $F \cap\{$ Prime numbers $\}=\varnothing$
(iv) $n(F)=8$
(ix) $\quad 36 \in S \cap F^{\prime}$
( v ) $n(S \cap F)=6$
( $\mathbf{x}$ ) $\quad 3 \notin S \cup F$
[ 14 marks ]

