Iteration

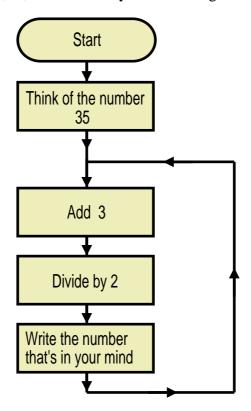
7.1 Revision

Non-Calculator

Marks Available: 60

Question 1

A number sequence, U, is described by the following flowchart,



Complete this table to show the first six terms in sequence U

U_1	U_2	U_3	${U}_4$	U_5	U_6
35					
33					

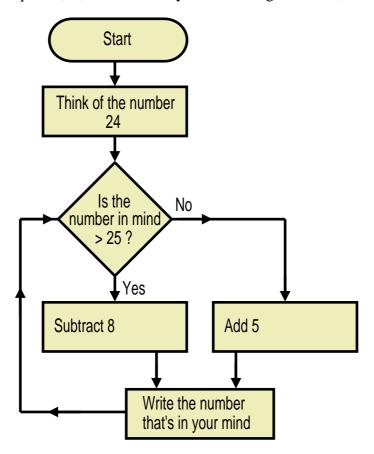
[7 marks]

Question 2

Simplify,

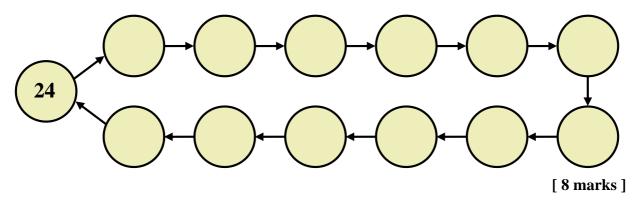
(i)
$$9 \times \left(\frac{5}{9} + 3\right)$$
 (ii) $\left(8 + \frac{3}{4}\right) \times 4$

A number sequence, K, is described by the following flowchart,



The flowchart generates a loop of numbers.

On the following diagram write out the numbers that are in the loop.



Question 4

First expand the brackets, then simplify,

(i)
$$\left(3 + \frac{2}{7}\right) \times 7$$

[2 marks]

(ii)
$$\frac{\left(3+\frac{2}{7}\right)}{1}\times\frac{7}{7}$$

[2 marks]

A sequence of numbers has the iterative rule

$$A_1 = \frac{1}{9} \qquad A_{n+1} = \frac{3}{2} A_n$$

Use the space below to work out the first six terms of this iterative sequence. Simplify fractions where possible.

Put your answers in the table.

A_1	A_2	A_3	A_4	A_5	A_6

[7 marks]

Question 6

Simplify,

$$(\mathbf{i}) \qquad \frac{\left(\frac{3}{11} + 2\right)}{6} \times \frac{11}{11}$$

[2 marks]

$$(\mathbf{ii}) \qquad \frac{\left(5 + \frac{7}{9}\right)}{7}$$

[2 marks]

(iii)
$$\frac{\left(4+\frac{3}{7}\right)}{7}$$

[2 marks]

(i) The following sum has an answer that is a rational number.

That is, a number in the form $\frac{p}{q}$ for integer p and q with $q \neq 0$

Determine what that rational number is.

$$\frac{\left(4-\frac{3}{2}\right)}{2}$$

[2 marks]

(ii) Consider the iteration,
$$B_1 = 1$$
, $B_{n+1} = \frac{4 - B_n}{2}$

Use the space below to work out the first six terms of this iterative sequence and put your answers in the table towards the bottom of the page.

B_1	B_2	B_3	B_4	B_5	B_6

[7 marks]

Question 8

Simplify,

$$(\mathbf{i}) \qquad \frac{1}{\left(\frac{5}{3}+1\right)} \times \frac{3}{3}$$

[2 marks]

$$(\mathbf{ii}) \qquad \frac{4}{\left(\frac{2}{7}+3\right)}$$

[2 marks]

$$(\mathbf{iii}) \qquad \frac{2}{\left(\frac{7}{10} + 5\right)}$$

[2 marks]

(i) The following sum has an answer that is a rational number.

That is, a number in the form $\frac{p}{q}$ for integer p and q with $q \neq 0$

Determine what that rational number is.

$$\frac{1}{\left(\frac{2}{5}+1\right)}$$

[2 marks]

(ii) Consider the iteration,
$$Z_1 = 4$$
, $Z_{n+1} = \frac{2}{Z_n + 1}$

Use the space below to work out the first six terms of this iterative sequence and put your answers in the table towards the bottom of the page.

Z_1	Z_2	Z_3	Z_4	Z_5	Z_6

[7 marks]