

## Lesson 2

### The Normal Distribution A-Level Applied Mathematics : Statistics : Year 2

#### 2.1 Easy Problems On The Normal Distribution

##### Example N° 1

The weights of packets of *Woofertific*<sup>TM</sup> dog biscuits are normally distributed with mean 625 g and standard deviation 15 g. What is the probability that the contents of a randomly selected packet of *Woofertific*<sup>TM</sup> weigh more than 630 g ?

##### Example N° 2

The time in seconds to react to an emergency alarm in an aircraft simulator is found from experience to be normally distributed with  $X \sim N(1.64, 0.7^2)$ .

Pilots with the quickest 4% of reaction times are said to be 'sharp'.

( i ) What is the longest reaction time that will result in a pilot being 'sharp' ?

Pilots with the slowest 4% of reaction times are said to be 'wrecked'.

( ii ) What is the shortest reaction time that will result in a pilot being 'wrecked' ?

## 2.2 Exercise

### Question 1

The volume of anti-bacterial hand wash dispensed by an anti-bacterial hand wash dispenser on each press,  $X$  ml, is modelled as  $X \sim N(8, 0.6^2)$ .

Find (i)  $P(X > 9)$

(ii)  $P(X < 8.4)$

### Question 2

Boxes of chocolate with mean weight 1 kg are produced.

It is decided that all boxes weighing less than 990 g will be repacked.

Also, all boxes weighing more than 1050 g will be repacked.

If the weights of the boxes is normally distributed with standard deviation 20 g, what proportion of boxes are repacked?

**HINT :** Draw a diagram and try to spot the 'clever' way of answering this question.

**Question 3**

*S1 Examination question from June 2003, Q2*

The lifetimes of batteries used for a computer game have a mean of 12 hours and a standard deviation of 3 hours.

Battery lifetimes may be assumed to be normally distributed.

Find the lifetime,  $t$  hours, of a battery such that 1 battery in 5 will have a lifetime longer than  $t$ .

[ 6 marks ]

**Question 4**

*S1 Examination question from June 2005, Q6*

A scientist found that the time taken,  $M$  minutes, to carry out an experiment can be modelled by a normal random variable with mean 155 minutes and standard deviation 3.5 minutes

Find ( a )  $P ( M > 160 )$

[ 3 marks ]

( b )  $P ( 150 \leq M \leq 157 )$

[ 4 marks ]

( c ) the value of  $m$  to 1 decimal place, such that  $P ( M \leq m ) = 0.30$

[ 4 marks ]

**Question 5**

*SI Examination question from June 2007, Q6*

The random variable  $X$  has normal distribution with mean 20 and standard deviation 4

( a ) Find  $P ( X > 25 )$

[ 3 marks ]

( b ) Find the value of  $d$  such that  $P ( 20 < X \leq d ) = 0.4641$

[ 4 marks ]

**Question 6**

*SI Examination question from May 2011, Q4*

Past records show that the times, in seconds, taken to run 100 m by children at a school can be modelled by a normal distribution with a mean of 16.12 and a standard deviation of 1.60

A child from the school is selected at random

( a ) find the probability that this child runs 100 m in less than 15 s

[ 3 marks ]

On sports day the school awards certificates to the fastest 30% of children in the 100 m race

( b ) Estimate, to 2 decimal places, the slowest time taken to run 100 m for which a child will be awarded a certificate

[ 4 marks ]

**Question 7**

*S1 Examination question from January 2012, Q7*

A manufacturer fills jars with coffee.

The weight of coffee,  $W$  grams, in a jar can be modelled by a normal distribution with mean 232 grams and standard deviation 5 grams

( a ) Find  $P ( W < 224 )$

[ 3 marks ]

( b ) Find the value of  $w$  such that  $P ( 232 < W < w ) = 0.20$

[ 4 marks ]

Two jars of coffee are selected at random

( c ) Find the probability that only one of the jars contains between 232 grams and  $w$  grams of coffee

[ 3 marks ]

**Question 8**

*S1 Examination question from June 2014, Q7*

The heights of adult females are normally distributed with mean 160 cm and standard deviation 8 cm

- ( a ) Find the probability that a randomly selected adult female has a height greater than 170 cm

[ 3 marks ]

Any adult female whose height is greater than 170 cm is defined as tall

An adult female is chosen at random.

Given that she is tall,

- ( b ) find the probability that she has a height greater than 180 cm

[ 4 marks ]

Half of tall adult females have a height greater than  $h$  cm

- ( c ) find the value of  $h$

[ 5 marks ]