**Year 2** Pure Mathematics Examination Revision : Health Check N° 6



## Your Prescription Is Attached

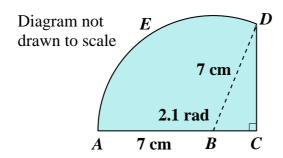
Any solution based entirely on graphical or numerical methods is not acceptable

Marks Available: 30

## **Question 1**

Differentiate  $\frac{x^4}{\cos 3x}$  with respect to x

## **Question 2**A-Level Examination Question from May 2014, Paper C2, Q5 (Edexcel)



The diagram shows the shape ABCDEA which consists of a right-angled triangle BCD joined to a sector ABDEA of a circle with radius 7 cm and centre.

A, B and C lie on a straight line with AB = 7 cm.

Given that the size of angle ABD is exactly 2.1 radians,

(a) find, in cm, the length of the arc DEA

[ 2 marks ]

(**b**) find, in cm, the perimeter of the shape *ABCDEA*, giving your answer to 1 decimal place

## **Question 3**

(a) Express  $12 \sin x + 5 \cos x$  in the form  $R \sin (x + \alpha)$ , where R and  $\alpha$  are constants R > 0 and  $0 < \alpha < 90^{\circ}$ . Round  $\alpha$  to 1 decimal place.

[4 marks]

A runner's speed, v in m/s, in an endurance race can be modelled by the equation,

$$v(x) = \frac{50}{12\sin\left(\frac{2x}{5}\right)^{\circ} + 5\cos\left(\frac{2x}{5}\right)^{\circ}}, \ 0 \le x \le 300$$

where *x* is the time in minutes since the beginning of the race.

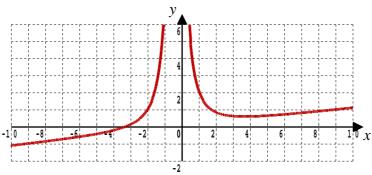
(**b**) Find the minimum value of v

[2 marks]

(c) Find the time into the race when this speed occurs.

[ 1 mark ]

**Question 4** 



The graph is of the function,

$$f(x) = \frac{32}{(3x+1)^2} + \frac{x}{9}$$

Find the exact value of x at the minimum point.

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A-Level Examination Question from June 2017, Paper C3, Q9 (Edexcel)

(a) Prove that  $\sin 2x - \tan x = \tan x \cos 2x$ ,  $x \neq (2n+1)90^{\circ}$ ,  $n \in \mathbb{Z}$ 

[4 marks]

(**b**) Given that  $x \neq 90^{\circ}$  and  $x \neq 270^{\circ}$ , solve, for  $0 \leq x < 360^{\circ}$  $\sin 2x - \tan x = 3 \tan x \sin x$ 

Give your answers in degrees to one decimal place where appropriate.

[ **5** marks ]